



Lecture 6

Texture mapping

Skyboxes

Environment mapping

Bump mapping



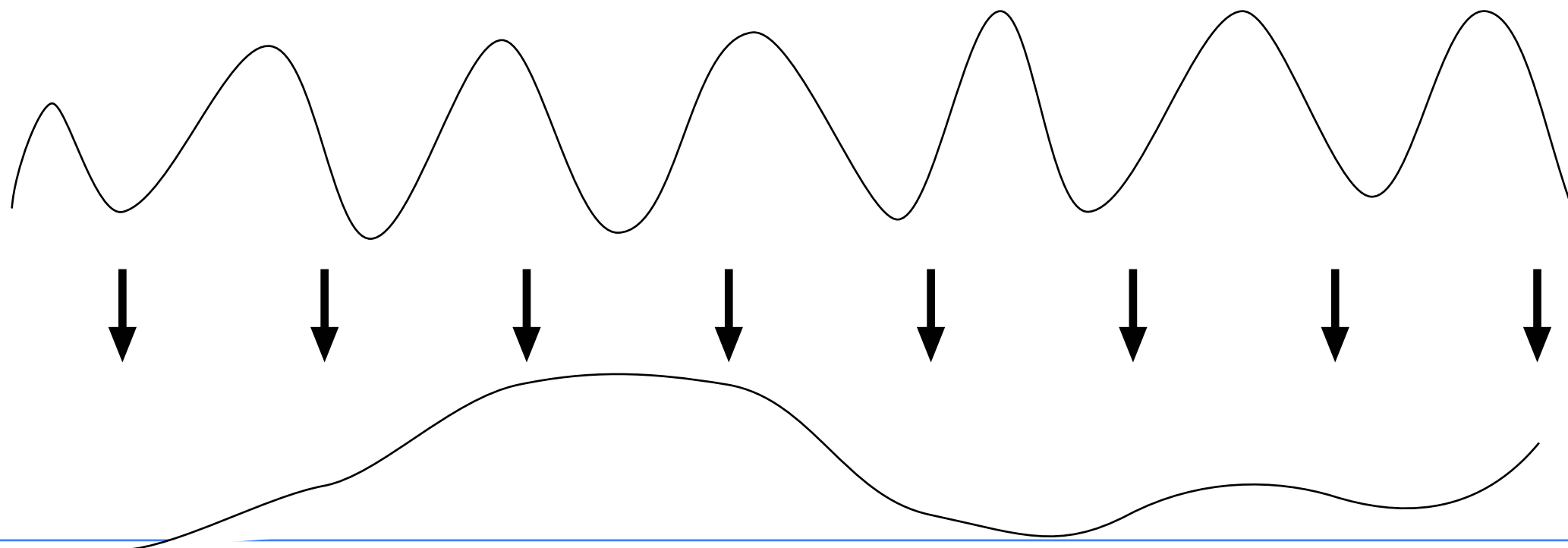
Lecture questions

1. What happens if you access outside a texture?
2. How can you generate texture coordinates?
3. In multitexturing, how can you decide what texture to use?
4. How big is a skybox?
5. When do we get aliasing problems in graphics?



Aliasing

A digital image is a sampled signal
If the signal is not band limited, aliasing will occur





Aliasing in texture mapping

At large distance, textures get smaller

=>

higher spatial frequencies on the screen

=>

increasing risk for aliasing!



Aliasing can be reduced by two methods:

Filtering

```
glTexParameteri(GL_TEXTURE_2D, GL_TEXTURE_MIN_FILTER,  
                GL_LINEAR);
```

Mip-mapping

```
glGenerateMipmap();
```

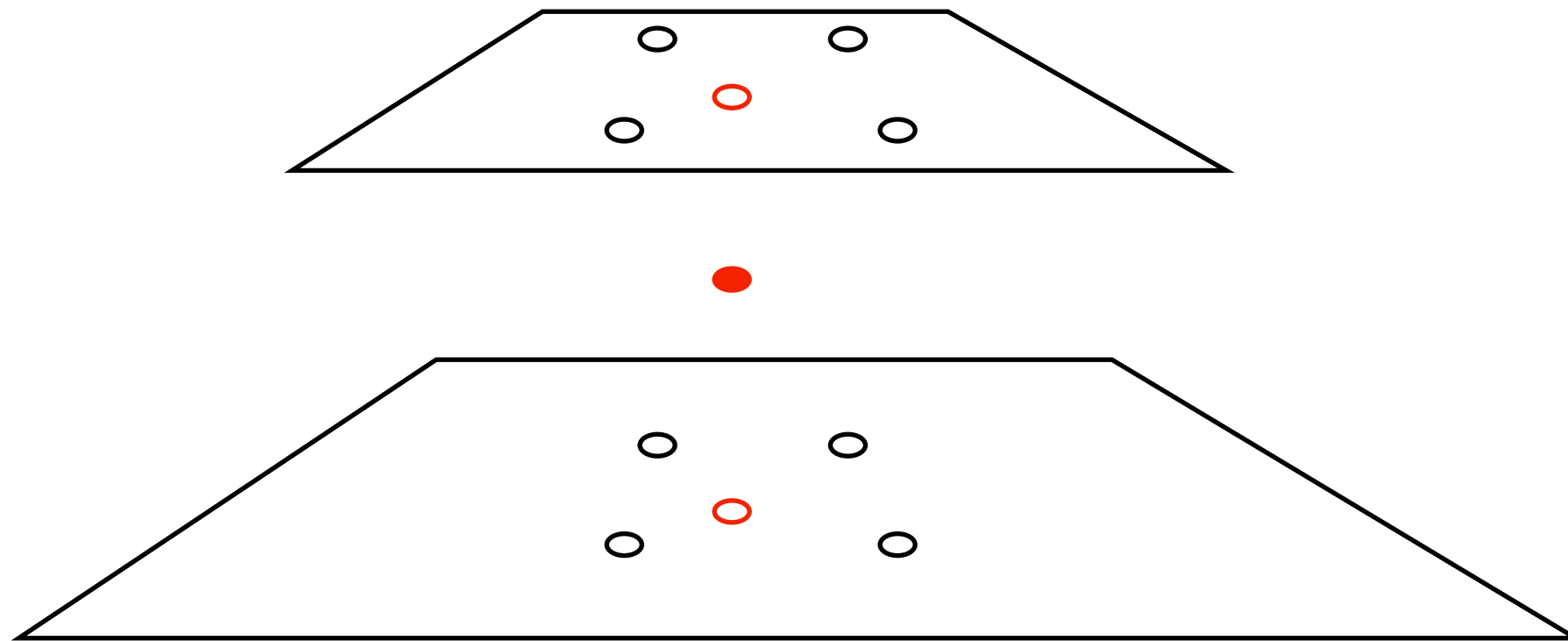
```
glTexParameteri(GL_TEXTURE_2D, GL_TEXTURE_MIN_FILTER,  
                GL_LINEAR_MIPMAP_NEAREST);
```

```
glTexParameteri(GL_TEXTURE_2D, GL_TEXTURE_MIN_FILTER,  
                GL_LINEAR_MIPMAP_LINEAR);
```




MIP mapping filtering

Both within a level and between!





MIP mapping filtering

GL_NEAREST
GL_LINEAR
GL_NEAREST_MIPMAP_NEAREST
GL_LINEAR_MIPMAP_NEAREST
GL_NEAREST_MIPMAP_LINEAR
GL_LINEAR_MIPMAP_LINEAR

Preferred:
GL_LINEAR for magnification
GL_LINEAR_MIPMAP_LINEAR for minification



MIP mapping

Gives anti-aliasing at a very low cost.

Good results in most situations.

Aliasing problems remain at steep angles.



Generating texture coordinates

Now we know how to draw, but... where do the texture coordinates come from?

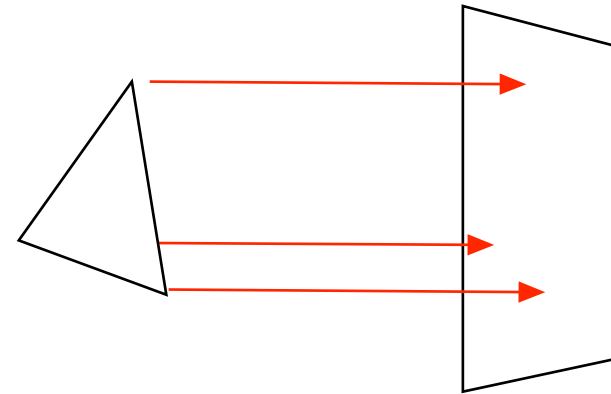
May be delivered with the model... but can we make them ourselves?

Yes!

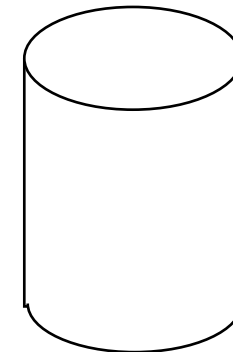


Common mappings

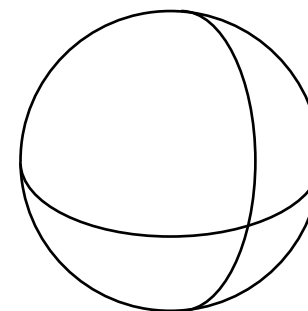
Planar



Cylinder



Sphere



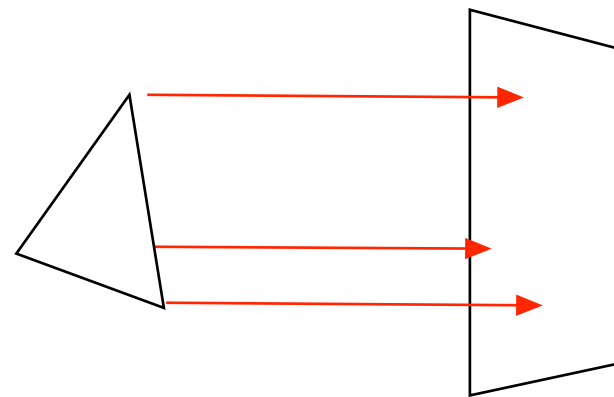


Planar texture mapping

Along z:

$$u = x$$

$$v = y$$





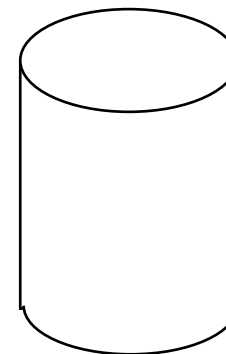
Cylindrical texture mapping

$$x = R \cos(\theta)$$

$$y = R \sin(\theta)$$

$$u = \theta = \arctan(y, x)$$

$$v = z$$



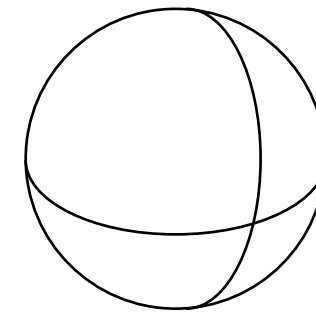
$$\begin{aligned} \arctan(y, x) = \\ x > 0: \tan^{-1}(y/x) \\ x < 0: \pi + \tan^{-1}(y/x) \\ x = 0, y > 0: \pi/2 \\ x = 0, y < 0: -\pi/2 \end{aligned}$$



Spherical texture mapping

$$\begin{aligned}x &= R \cos(\phi) \cos(\theta) \\y &= R \cos(\phi) \sin(\theta) \\z &= R \sin(\phi)\end{aligned}$$

$$\begin{aligned}u &= \arctan(y, x) \\v &= \sin^{-1}(z/R)\end{aligned}$$



(Swap $\cos(\phi)$ and $\sin(\phi)$ if you define ϕ from the z axis rather than from the equator!)

$$\begin{aligned}\arctan(y, x) &= \\x > 0: &\tan^{-1}(y/x) \\x < 0: &\pi + \tan^{-1}(y/x) \\x = 0, y > 0: &\pi/2 \\x = 0, y < 0: &-\pi/2\end{aligned}$$



$$(u,v) \Rightarrow (s,t)$$

Normalize, typically 0 to 1
Example: Cylinder

$$\begin{aligned} x &= R \cos(u) \\ y &= R \sin(u) \end{aligned}$$

$$\begin{aligned} u &= \arctan(y, x) \\ v &= z \end{aligned}$$

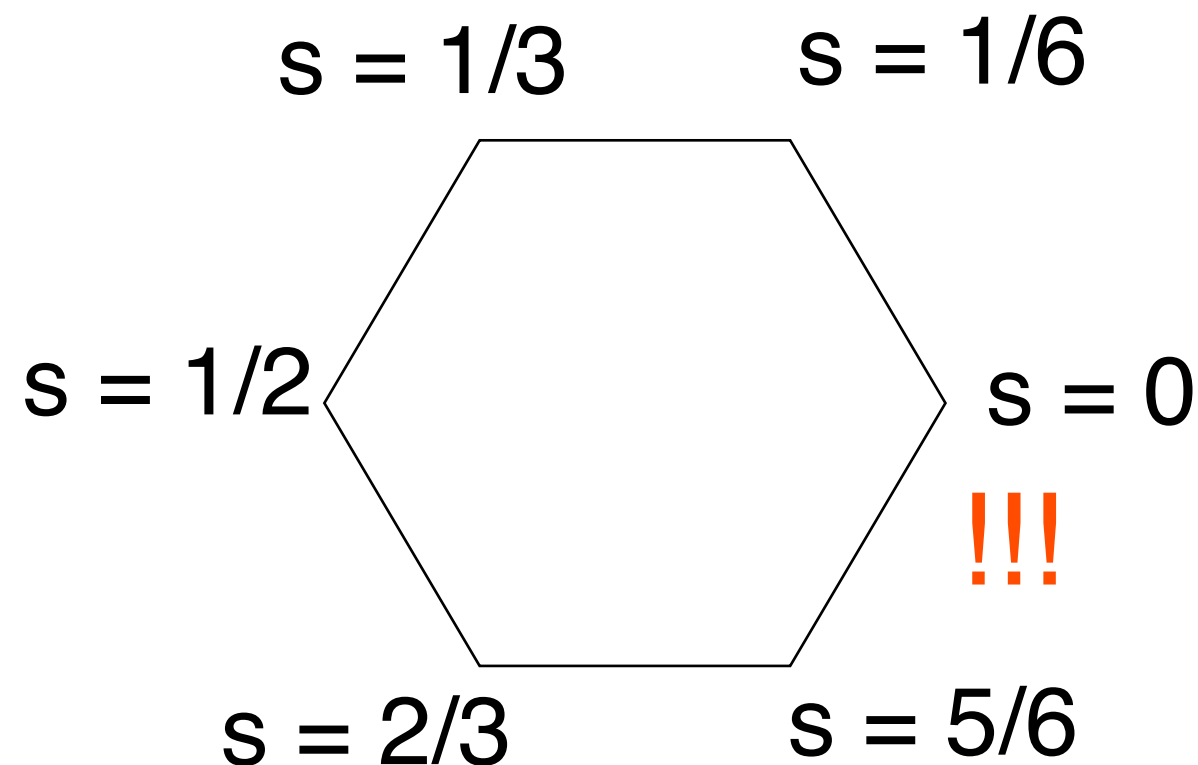
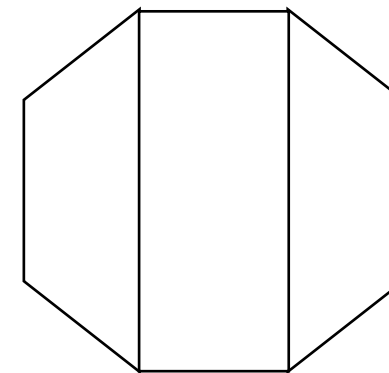
$$s = (u + \pi/2) / 2\pi$$

$$t = (v - z_{\min}) / (z_{\max} - z_{\min})$$



Watch the edges!

Example: six-sided barrel



$$\begin{aligned} x &= R \cos(u) \\ y &= R \sin(u) \end{aligned}$$

$$\begin{aligned} u &= \arctan(y, x) \\ v &= z \end{aligned}$$

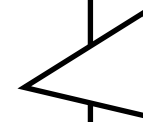
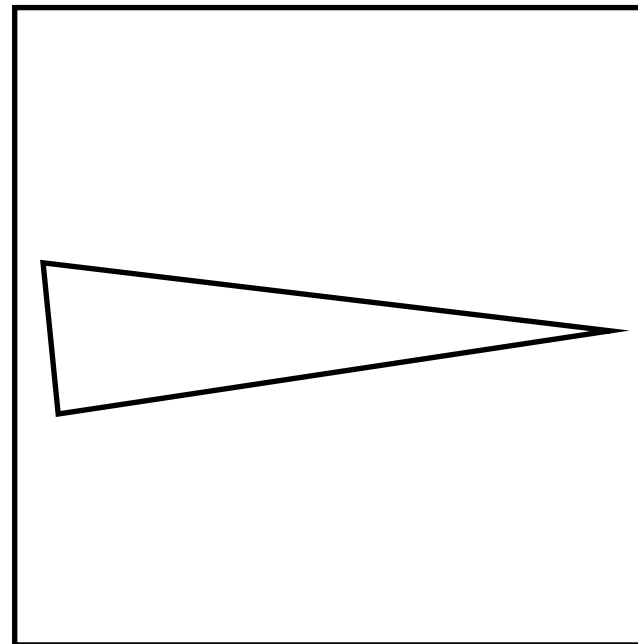
$$s = (u + \pi/2) / 2\pi$$

$$t = (v - z_{\min}) / (z_{\max} - z_{\min})$$

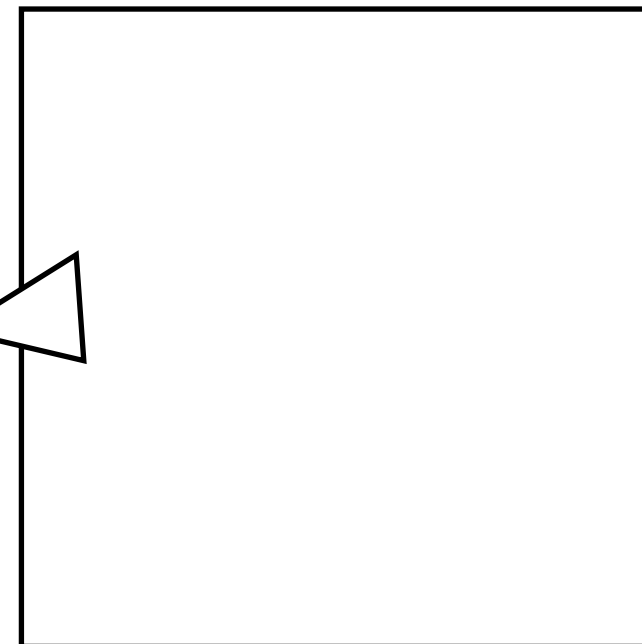


Problem is detected by checking proximity to the edge

Unlikely
(impossible)



Good



Duplicate vertices to solve



Multitexturing

The GPU has several texture units. Each texture unit can have one texture attached to it, available to the shader.

`glActiveTexture()` selects a texture unit to work on. Then `glBindTexture` can bind a texture to that unit.

You can use several texture units in the same fragment shader!
Just use multiple "sampler" variables.



Multitexturing applications

Bump mapping

Gloss mapping

Light mapping

Blending between textures (e.g. mountains)

Putting non-texture data in textures

Any case where you need more data than a single texture!



Multitexturing in GLSL

- Bind one texture per texturing unit
- Pass GLSL unit number and name
 - Declare as samplers in GLSL



Example: Multitexturing

(Lighting omitted, calculates light from two light sources, spec/spec2)

```
uniform sampler2D world;  
uniform sampler2D flower;  
out vec4 outColor;  
...  
float tot = diffuseStrength*0.2 + specularStrength*0.9;  
tot = max(0.0, tot);  
outColor = vec4(1.0 - tot) * world*0.7 + vec4(tot)* flower;
```




Texture mapping conclusions

Texture coordinates (s, t)

Texture objects and texture units

Filtering and mip-mapping

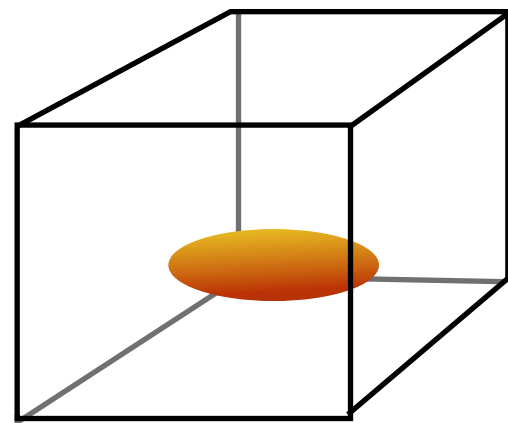
Texture coordinate generation

Multi-texturing

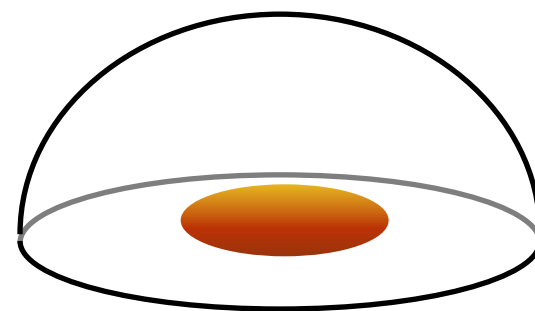


Skyboxes

A backdrop that makes your virtual world look bigger than it is.



Skybox



Skydome



Skyboxes

Infinite distance

=

the camera should always be in the center

=>

Always draw the skybox centered on the camera!



Skybox implementation

- Must be at infinite distance
 - Must follow camera
- Must rotate with world

How big should it be?



The skybox does not have to be big!

"Maximum size" will waste frustum space!

- Draw any size between "near" and "far" planes!
 - Draw with Z buffer turned off!

```
glDisable(GL_DEPTH_TEST);  
    Draw  
glEnable(GL_DEPTH_TEST);
```

Then anything else will be drawn on top!



More on skyboxes

- No light!

If you put light on a skybox, it will look like a box!

- Clamp to edge

Repeating textures will cause visible errors at edges!

(Why?)



Environment mapping

Reflects an environment texture in the surface

Mimicks mirroring reflections

In OpenGL:

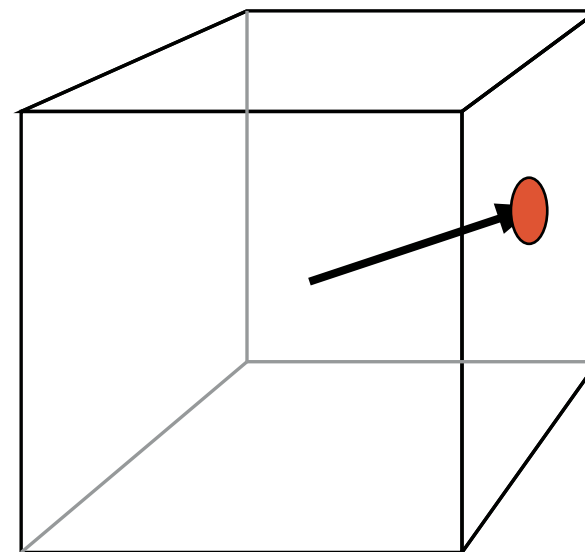
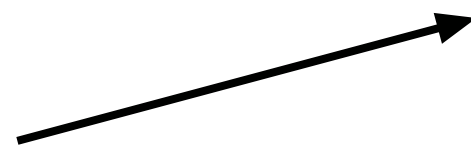
Spherical environment mapping (old)

Cube map environment mapping



Cube map lookup

Done with direction vector!

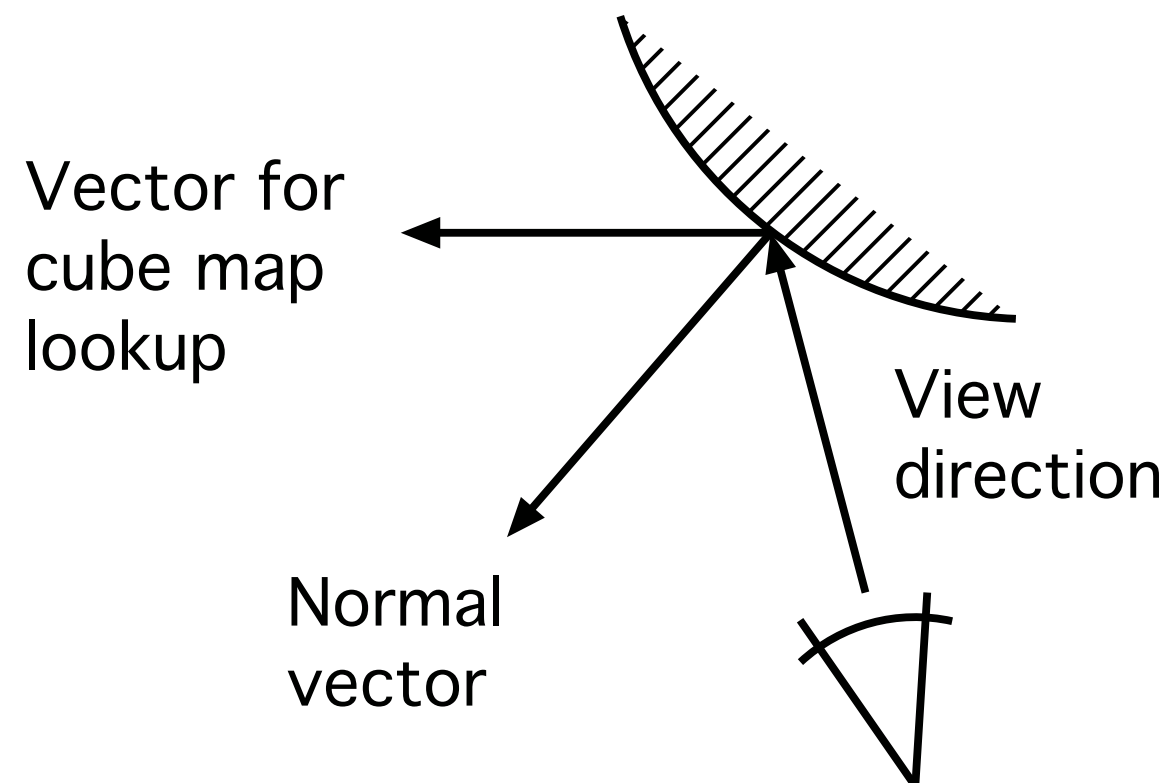


...is converted to a
position in the cube



Environment mapping with cube maps

Mirror view direction in surface to get direction vector



Can be done in vertex shader -> fast!



Bump mapping - the coordinate systems

Input:

A point p , normal vector n

Texture coordinates $s(p)$, $t(p)$

Directions of texture coordinates s , t

The bump function $b(s,t)$

Calculate the partial derivative of the bump function, b_s and b_t

$$n' = n + b_t * (s \times n) + b_s * (t \times n)$$

or, if s , t , n are orthogonal

$$n' = n + b_s * s + b_t * t$$



Texture coordinate system

How do we find the s and t vectors? We have the texture coordinates but no coordinate system!

Cross product with normal vector? With what?



Faking it

Cross product with absolutely anything!

$$s = x \times n / |x \times n|$$
$$t = n \times s$$

Works for some cases. (Noise bump maps in particular.

But we can do better!

