



Off-line rendering and global illumination

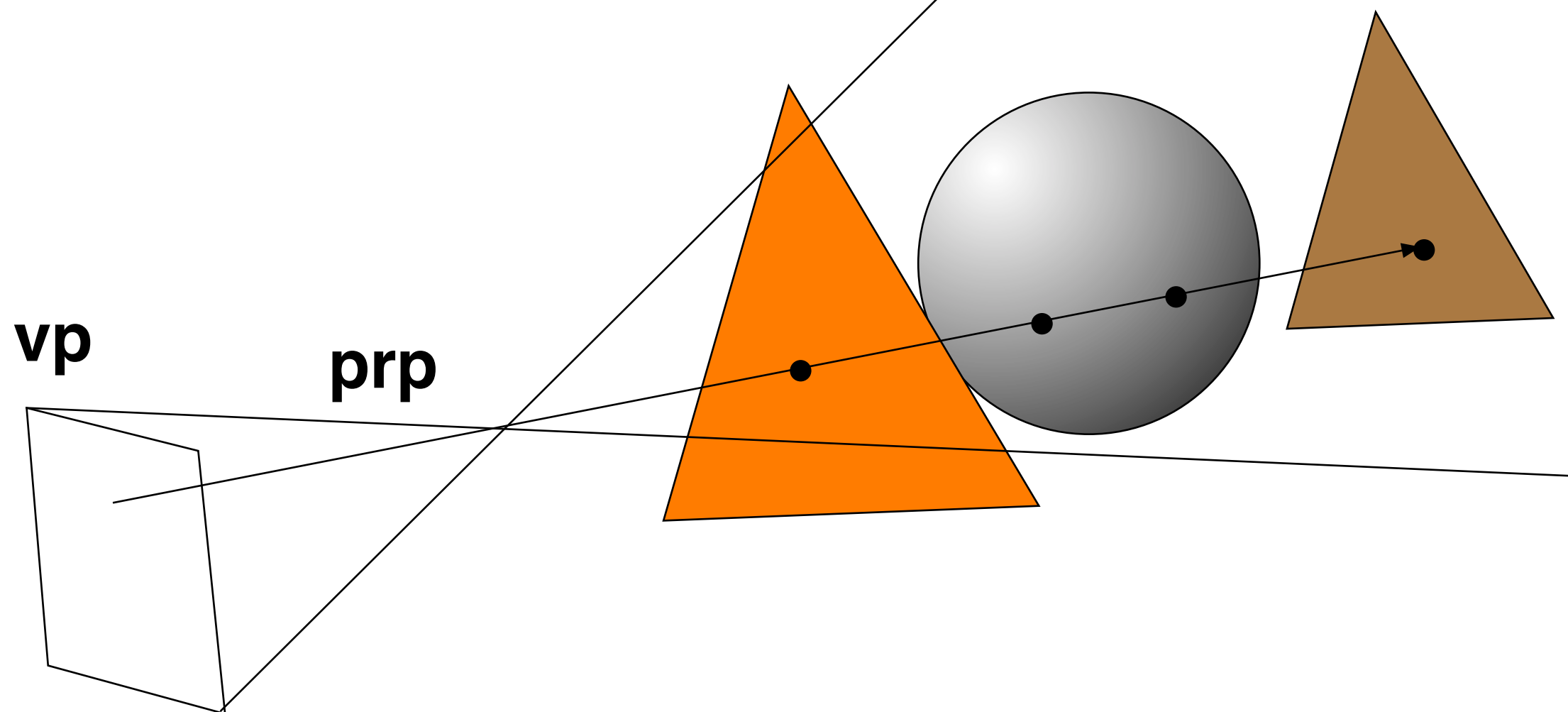
Performance demanding methods that give better lighting

Ray-casting
Radiosity
Photon mapping



Ray-casting

Follow rays from each pixel through the scene





Full 3D raycasting

for every pixel (x,y) in the image

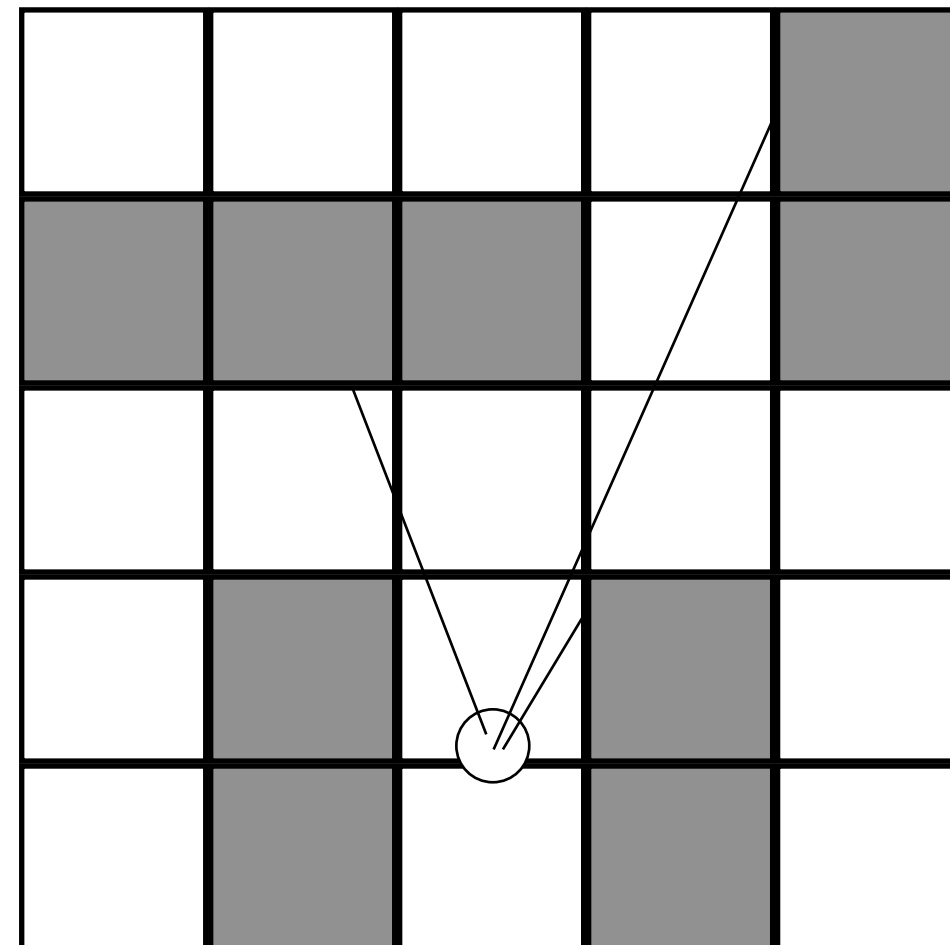
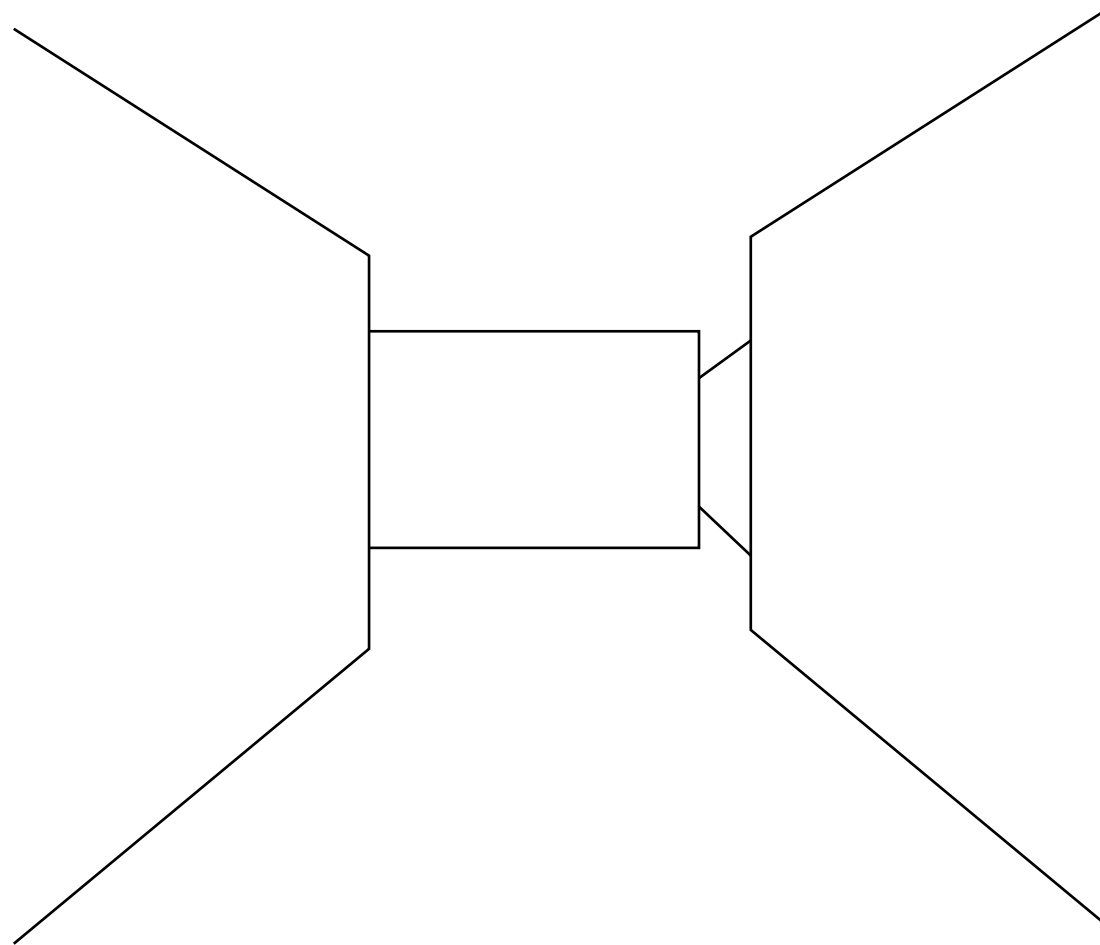
calculate a ray from the pixel through the camera (cop)
and through the scene

calculate intersecions with all objects in the scene

the pixel value is calculated from the closest
intersection found



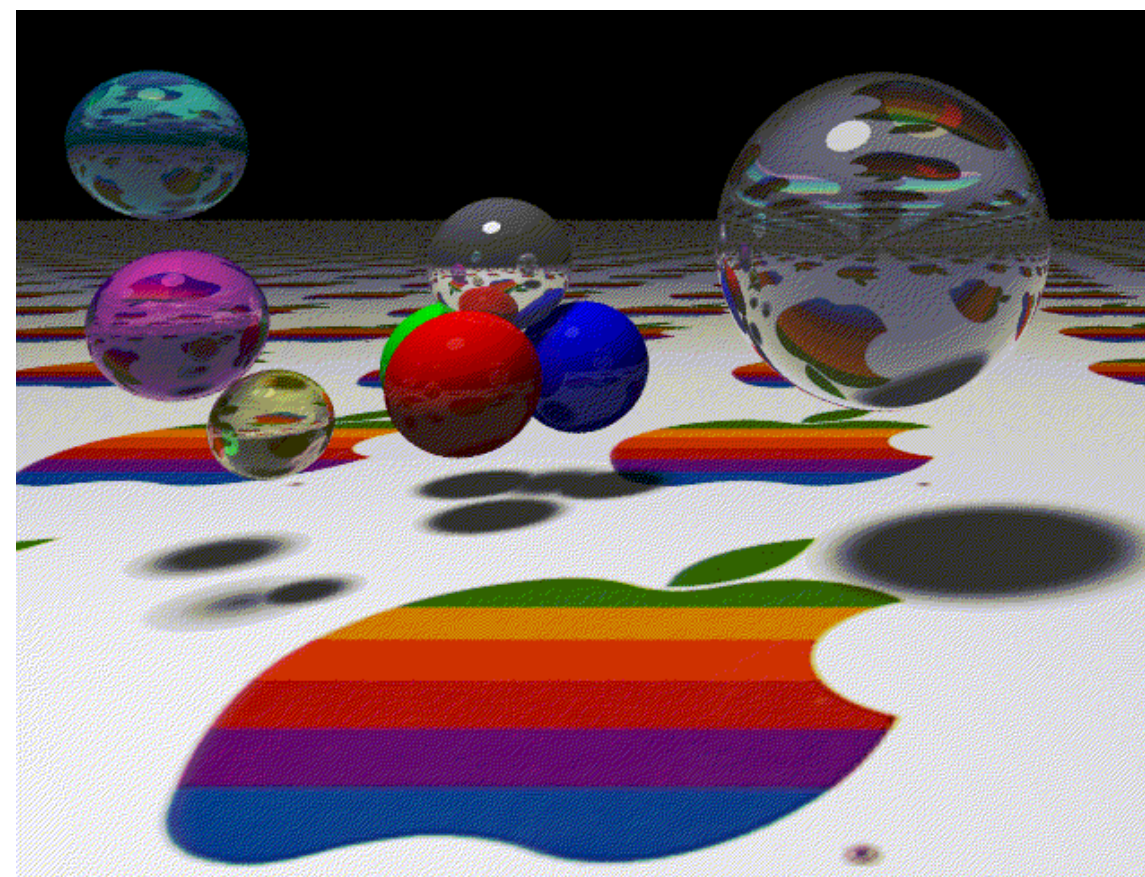
Raycasting in 2D grid ("Ray-marching")





Ray-tracing

The classic method for rendering realistic images of shiny and transparent objects.

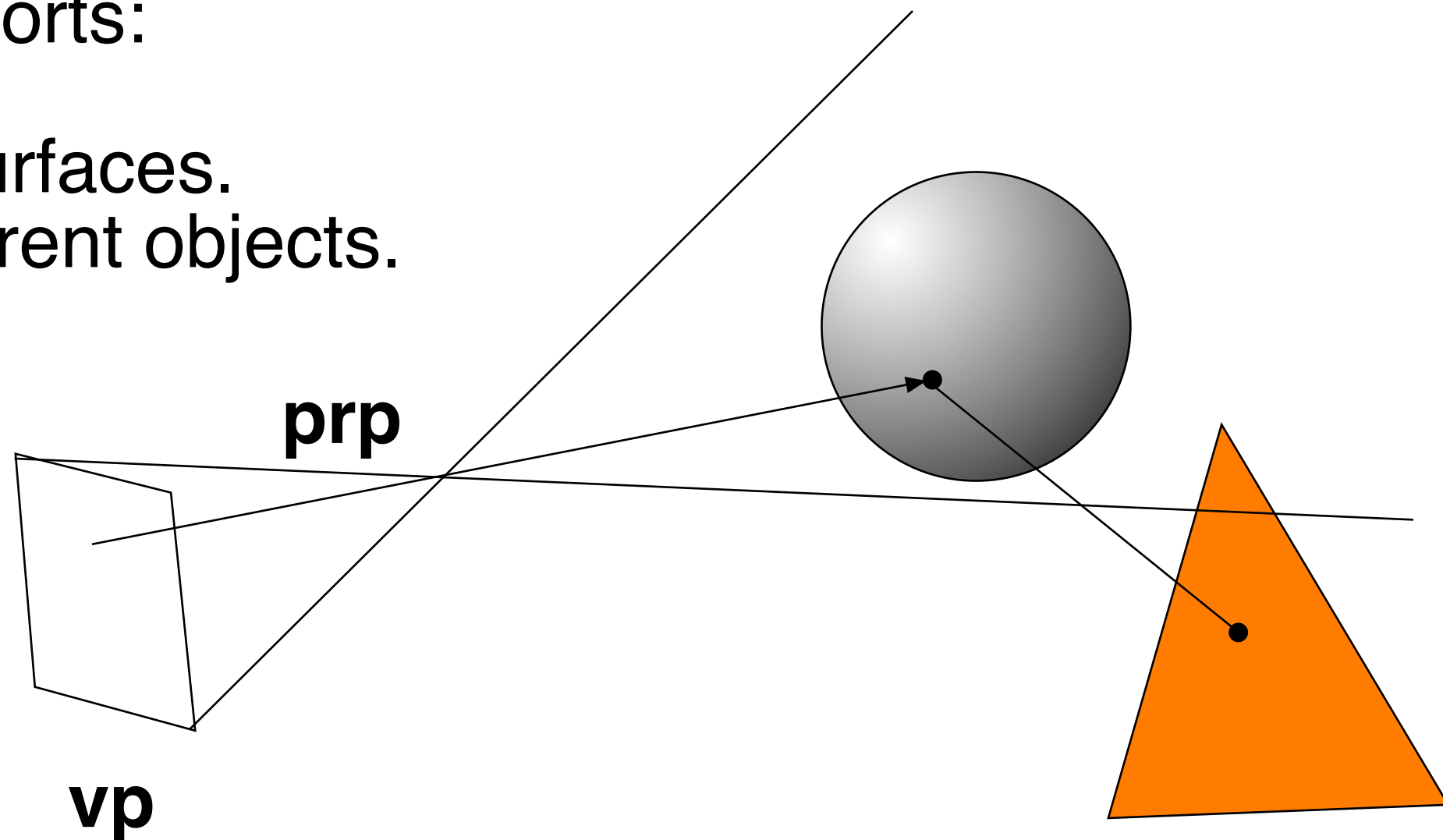




Ray-tracing

From some surfaces, follow rays to the next surface.
This supports:

- Shiny surfaces.
- Transparent objects.





At the intersection

Three things can happen when a ray intersects an object

1) Non-mirroring reflection

2) Reflection

3) Refraction



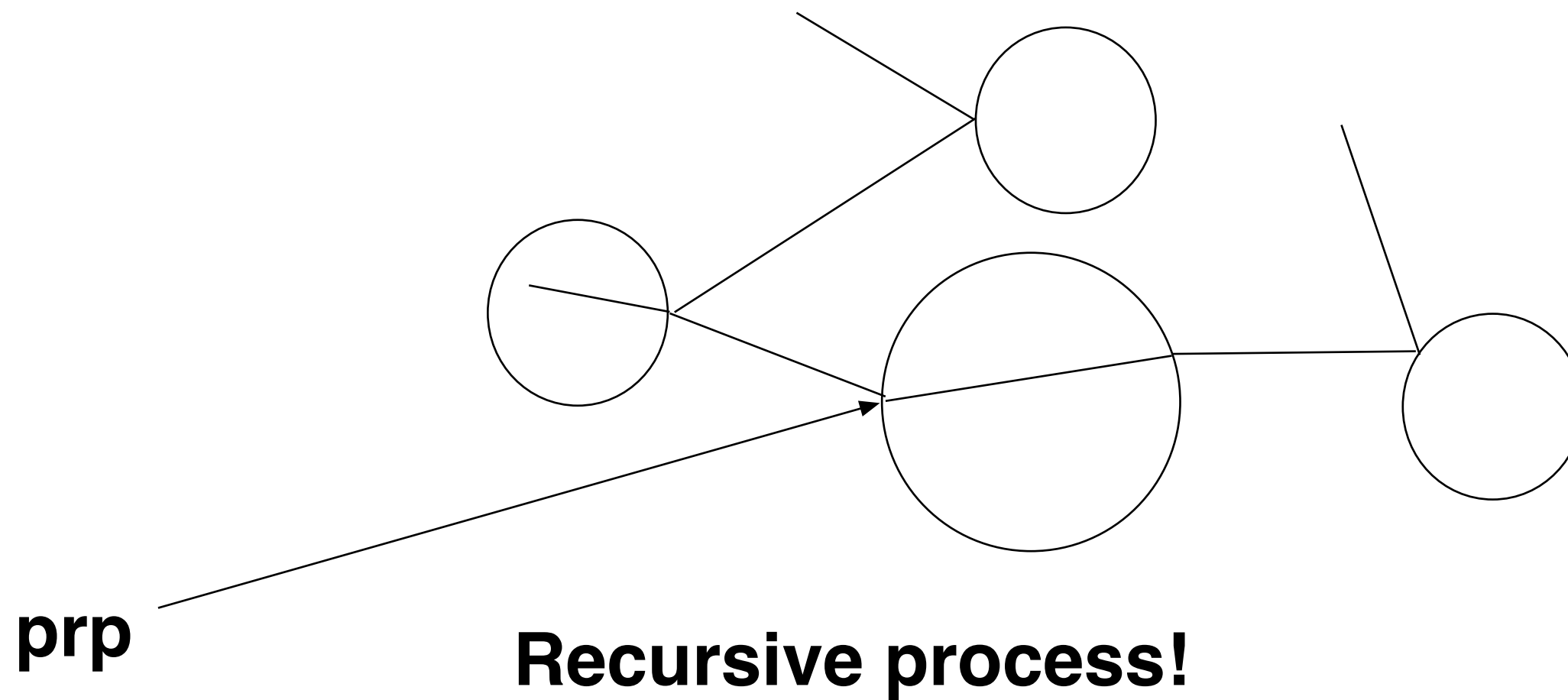
Non-mirroring reflection

Apply the three-component light model

Ambient light
Diffuse reflection
Specular reflection

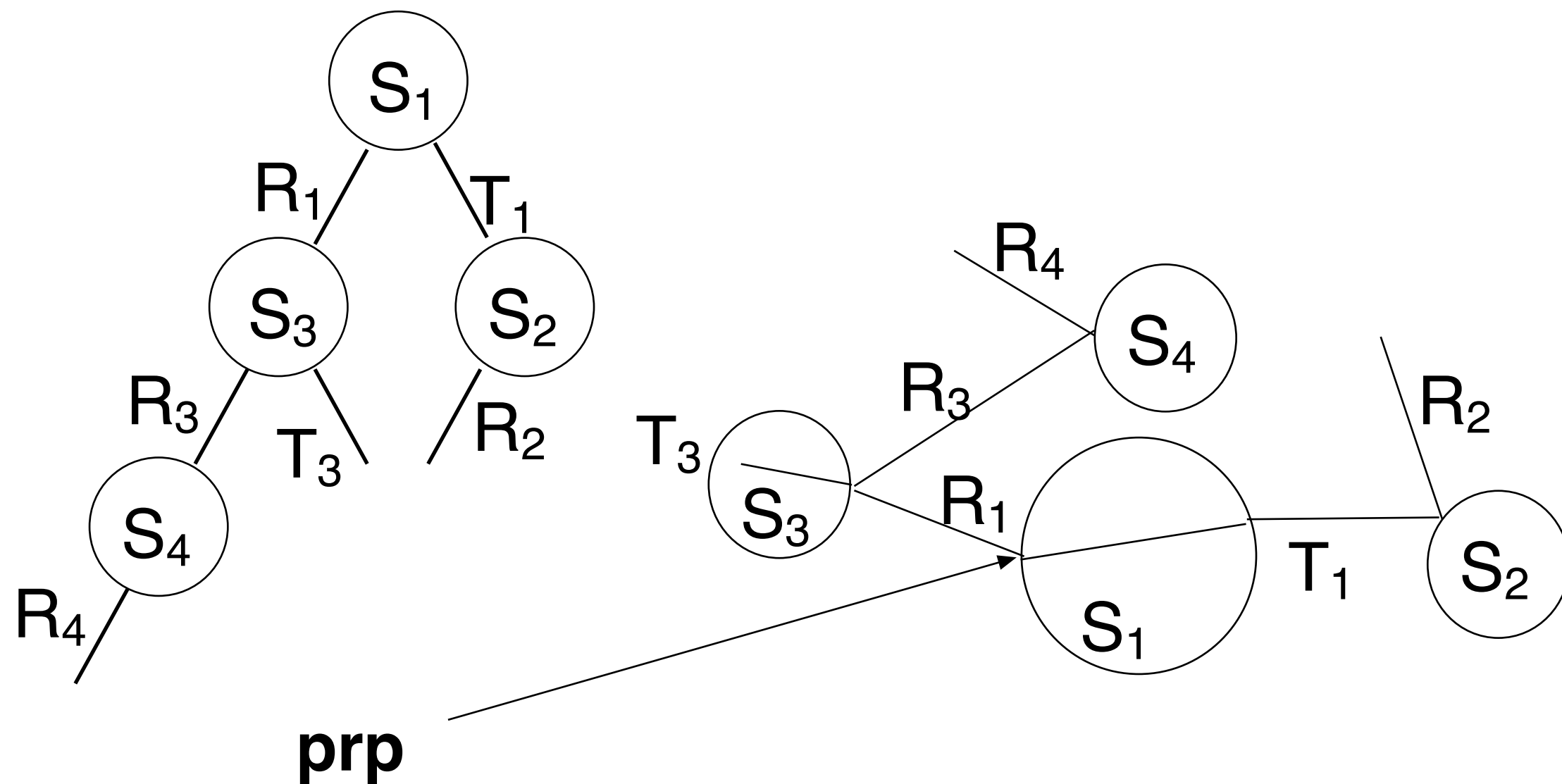


Reflection and refraction



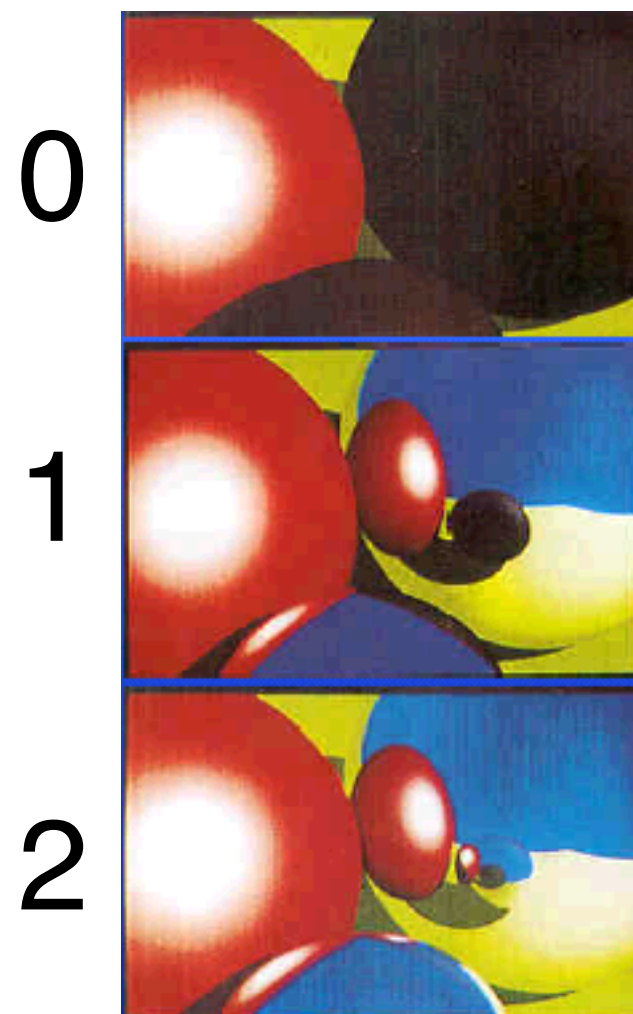


The ray-tracing tree



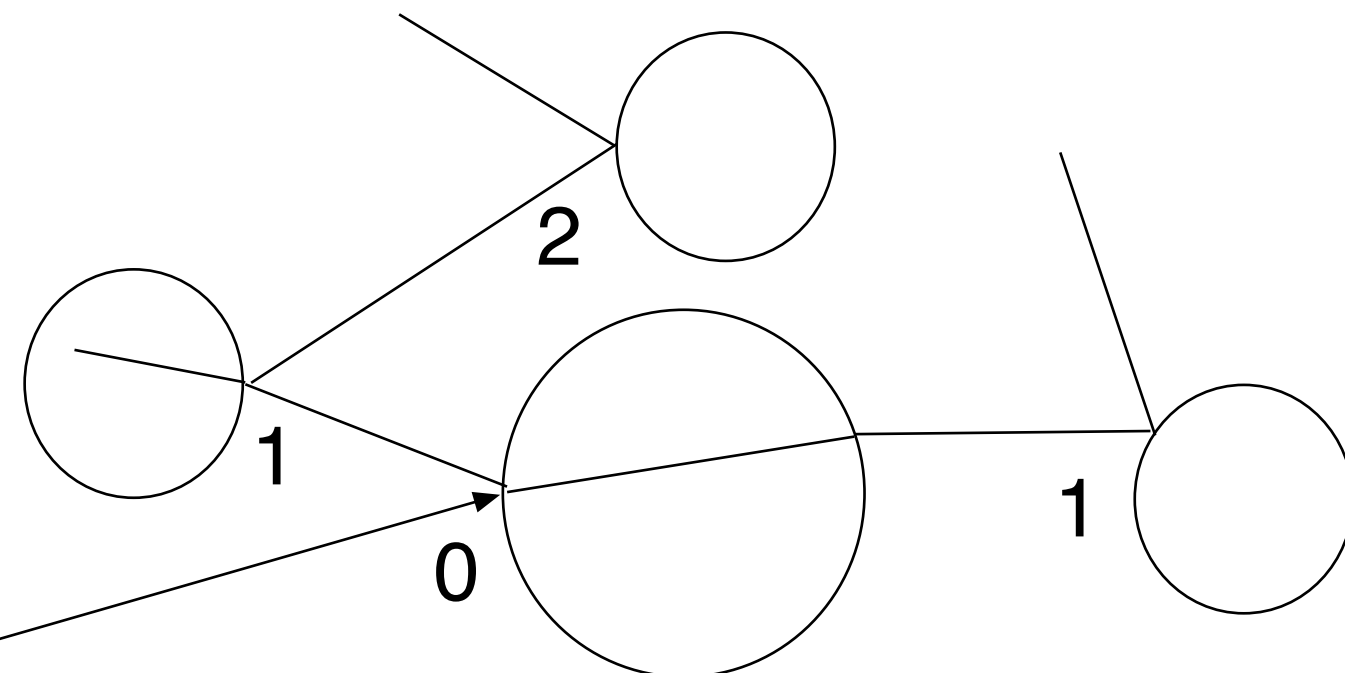


The maximum depth



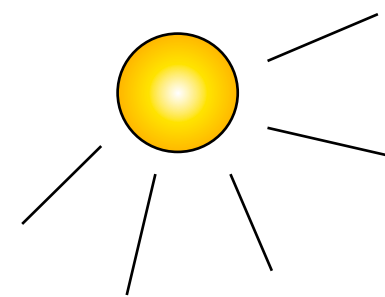
prp

**How deep can the tree get?
How many reflections and
refractions are allowed?**

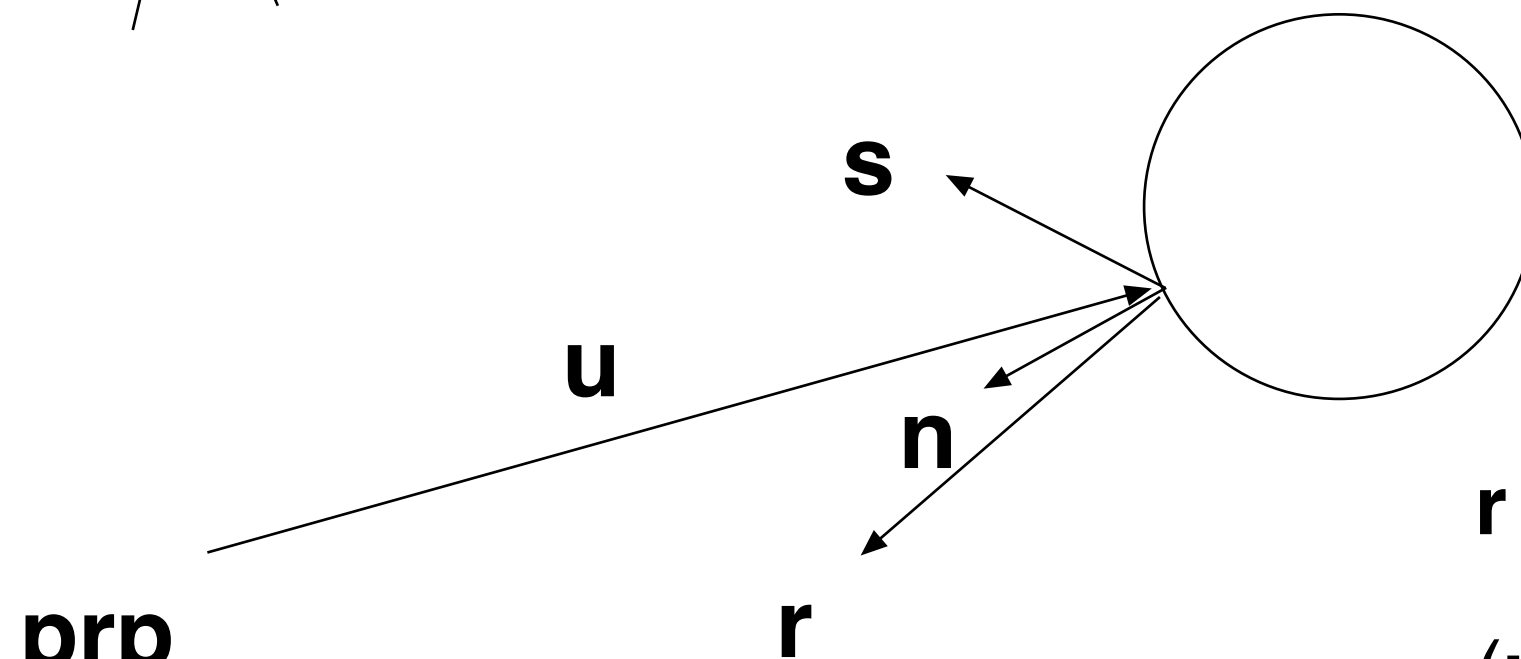




Reflections



Object with mirroring
reflection



$$\mathbf{r} = \mathbf{u} - (2\mathbf{u} \cdot \mathbf{n})\mathbf{n}$$

(\mathbf{u} = direction vector of the
incoming ray)



Refractions

Snell's law:

$$\eta_1 \sin\theta_1 = \eta_2 \sin\theta_2$$

Refraction index:

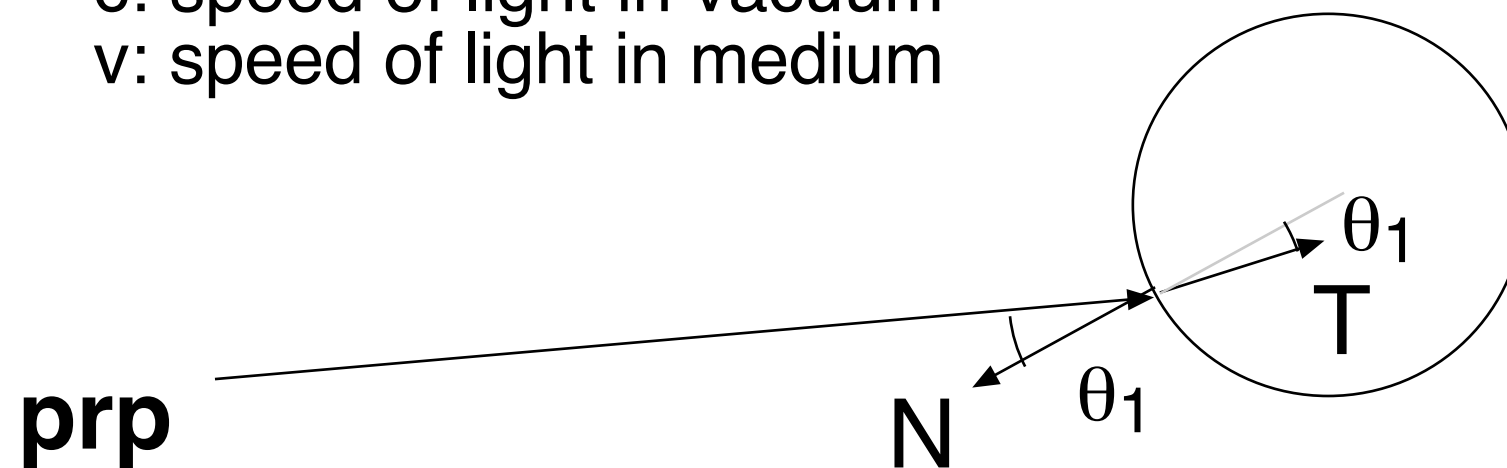
$$\eta = c / v$$

c: speed of light in vacuum

v: speed of light in medium

Transparent object

Look for more contributions here



Outgoing angle is given by incoming angles and the density of each material.



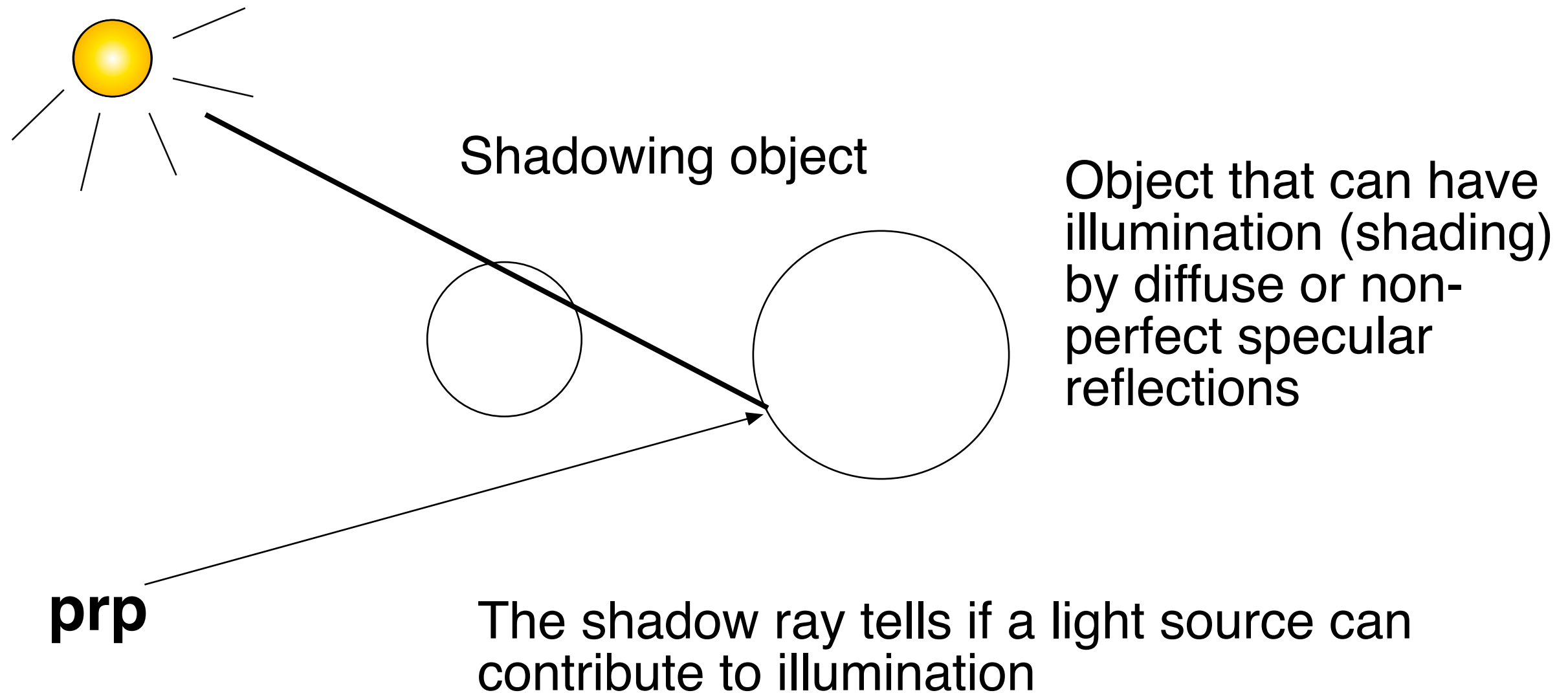
Summing up

The total intensity is the sum of

- **ambient light**
- **diffuse reflections from each light source**
- **specular reflections from each light source**
- **mirroring reflections**
- **refractions**



The shadow ray





Ray-surface intersections

Ray equation:

$$\mathbf{p} = \mathbf{p}_0 + \mu \mathbf{u}, \mu > 0$$

Combine with the equation of the surface.

Easiest surface: Sphere!

$$x^2 + y^2 + z^2 = r^2$$

Not quite as easy as for ray casting, since \mathbf{p}_0 can now be any point.



Information Coding / Computer Graphics, ISY, LiTH

```
function RayTrace(p0, u, depth)

if depth > max then return BLACK

 $\mu := \text{FindIntersection}(p0, u)$  // Returns more data, see below

if  $\mu \leq 0$  then return BACKGROUND_COLOR

Ilocal := 0
IR := 0
IT := 0

if  $k_a \neq 0$  and  $k_d \neq 0$  and  $k_s \neq 0$  then
  Ilocal :=  $k_a \cdot I_a + \sum$  (diffuse shading + specular shading)
  // Sum is for all visible light sources

if  $k_R \neq 0$  then
  R := CalculateReflection(u, N)
  IR := RayTrace(p0 +  $\mu \cdot u$ , R, depth+1)

if  $k_T \neq 0$  then
  T := CalculateRefraction(u, N, h1, h2)
  IT := RayTrace(p0 +  $\mu \cdot u$ , T, depth+1)

return Ilocal + IR + IT
```