



# **Lecture 13**

**Collision handling**

**Fractals**

**Noise functions, terrain generation**

**Self-squaring fractals**



# **Collision detection**

**Polyhedra-polyhedra in general NOT possible!**

**Multiple stages, broad phase/narrow phase**

**Simplify**

**Split shapes to convex parts**



**Simple cases:**

**Sphere - sphere**

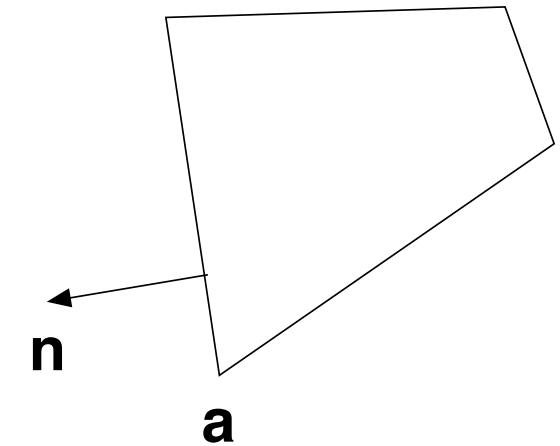
**Sphere - polyhedra**

**AABB - AABB**


$$\mathbf{n} \cdot (\mathbf{c} + r \cdot \mathbf{n}) > \mathbf{n} \cdot \mathbf{a}$$

$\Rightarrow$

$$r > \mathbf{n} \cdot (\mathbf{a} - \mathbf{c})$$



Distance from center to plane  $> r$

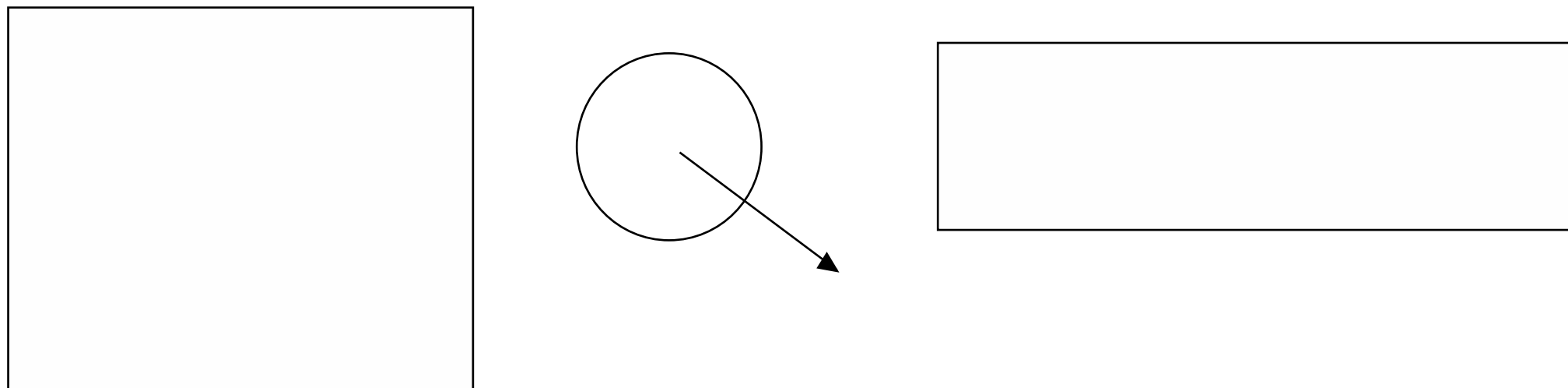
Valid when a line through  $\mathbf{c}$  along  $\mathbf{n}$  intersects the polygon!



# Collision detection & handling

**Simple case: Axis aligned 3D maze**

**All walls are AABBs All objects are spheres/cylinders**





## **Final notes on the simplified camera collisions:**

**Resolving: Pick the closest intersected plane as the one to "hit", and use that for collision handling. The smallest change is usually correct.**

**Conclusion: Don't overdo it if you can fake it. Be ambitious, but don't waste time on effects that nobody will notice.**



# Collision handling

**What to do once a collision is found.**

- **Separate**
- **Change velocities**
  - **Deform**
- **Maintain constraints**

**Full (narrow-phase) tests are hard to resolve.**



## Simple particle physics (again)

**acceleration = gravity + forces/mass**

**speed = speed + acceleration**

**position = position + speed**

$$\mathbf{a} = \mathbf{g} + \Sigma \mathbf{f}/m$$

$$\mathbf{s} = \mathbf{s} + \mathbf{a}$$

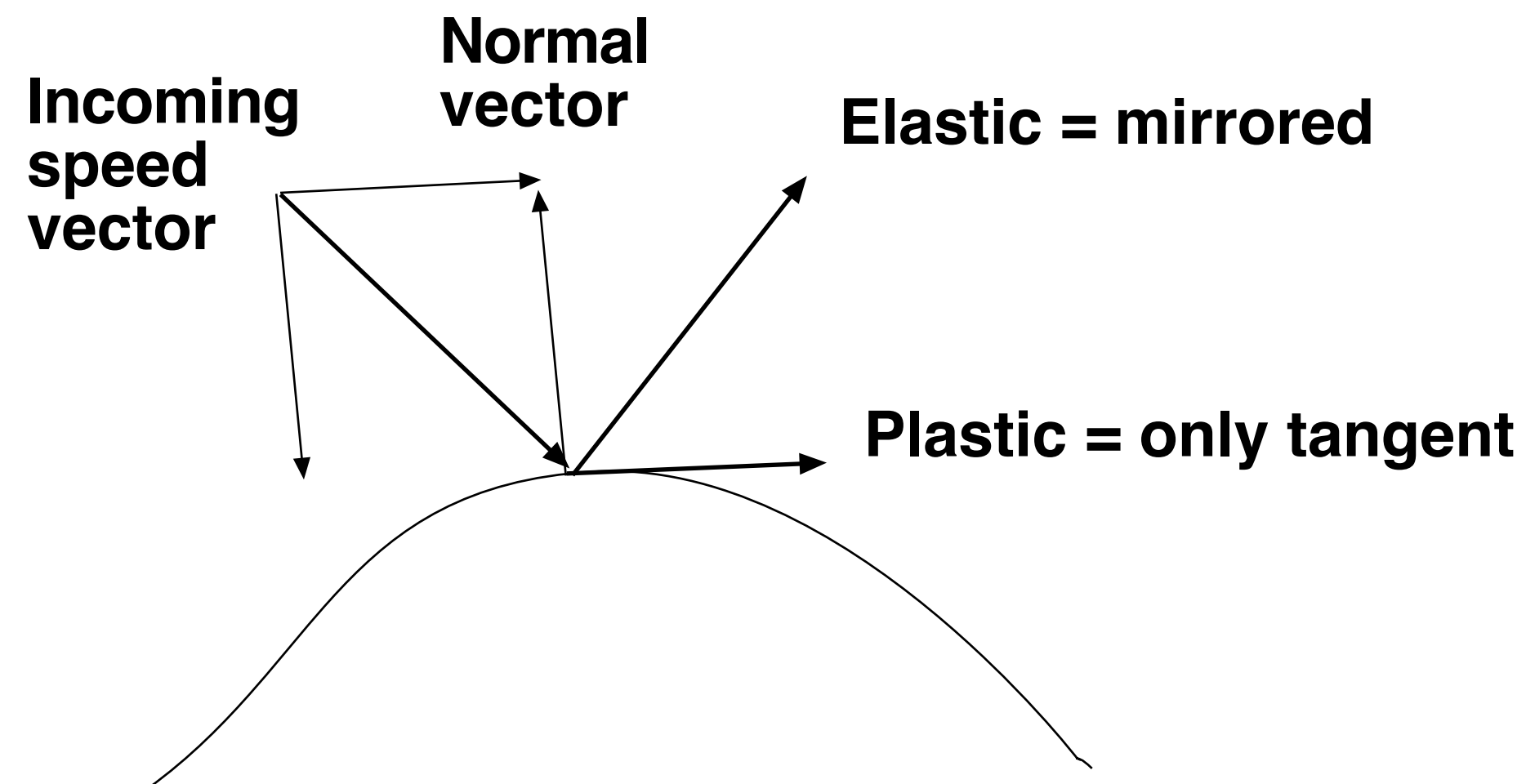
$$\mathbf{p} = \mathbf{p} + \mathbf{s}$$

**(“Euler integration”)**

**Modify speed and position in collisions**



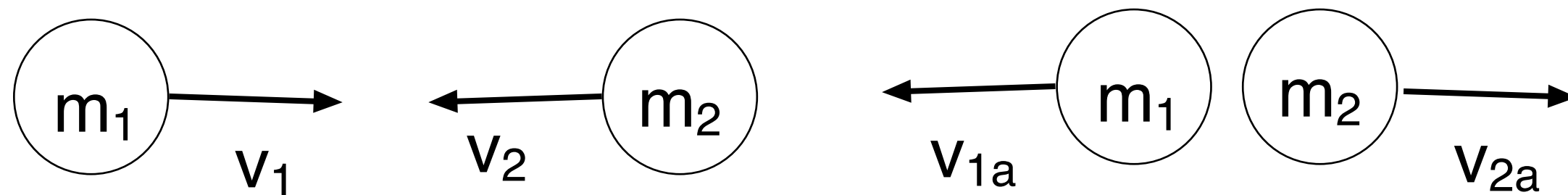
# Simple particle-surface collision







## Plastic and elastic collisions



**Preserve momentum**

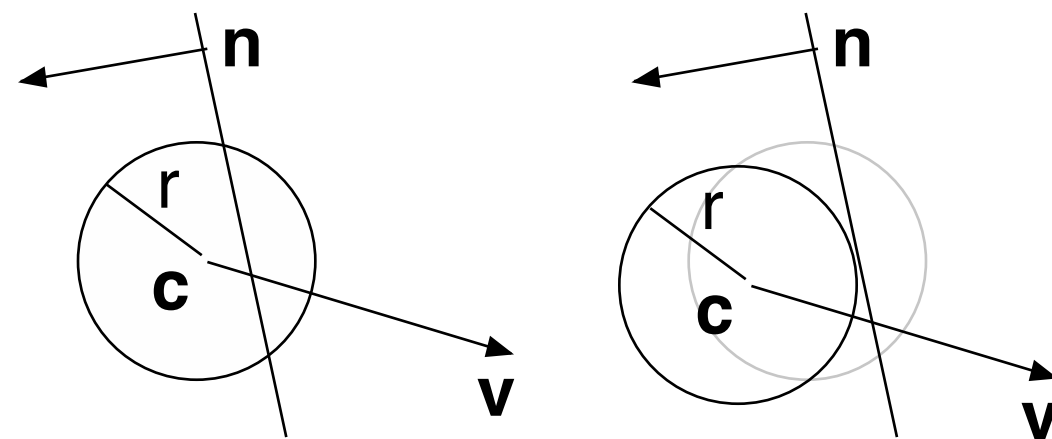
$$m_1 v_1 + m_2 v_2 = m_1 v_{1a} + m_2 v_{2a}$$

**Elastic collisions also preserve kinetic energy**

$$m_1 v_1^2 + m_2 v_2^2 = m_1 v_{1a}^2 + m_2 v_{2a}^2$$

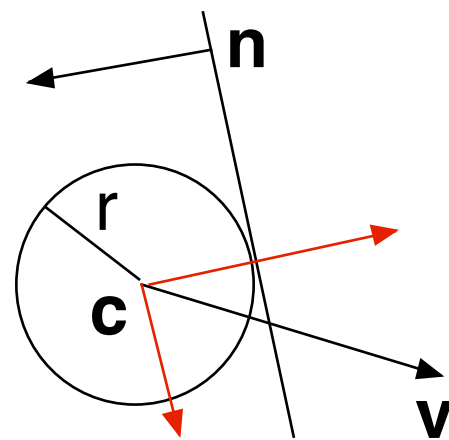


# Collision handling sphere-polyhedra

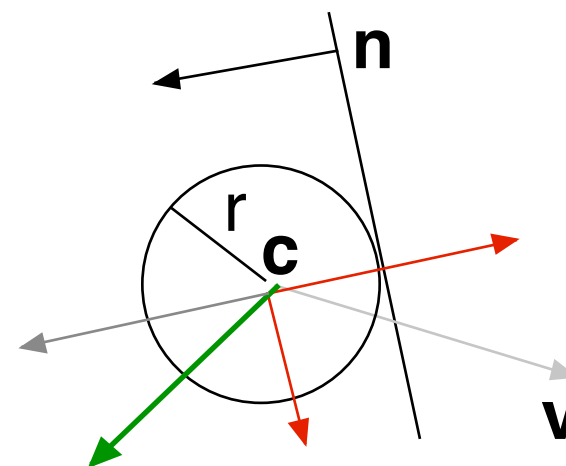


Assuming stationary polyhedra

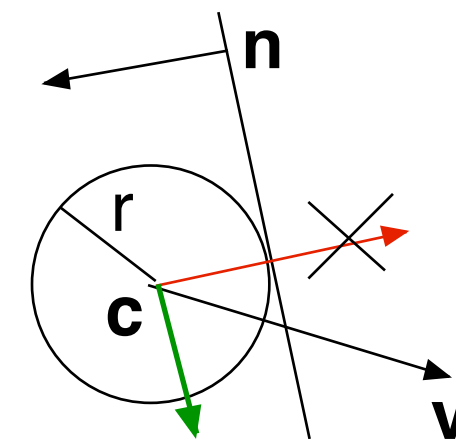
Separate - move object away along normal vector



Split velocity along  $n$



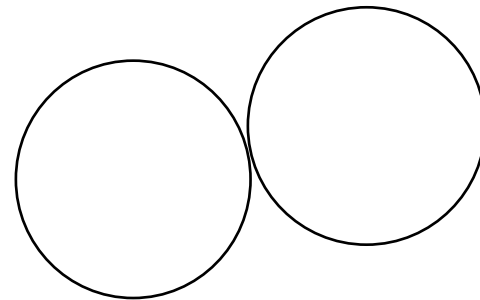
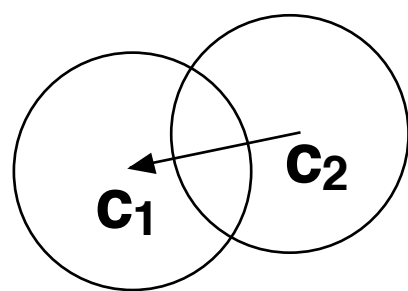
Elastic



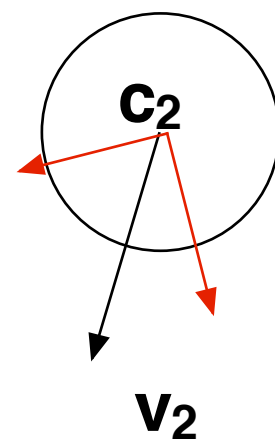
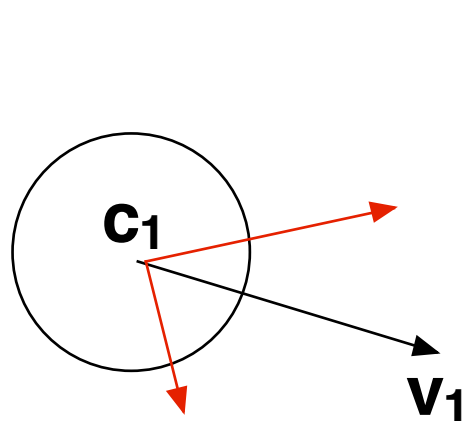
Plastic



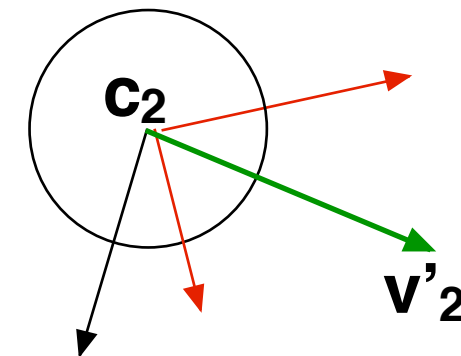
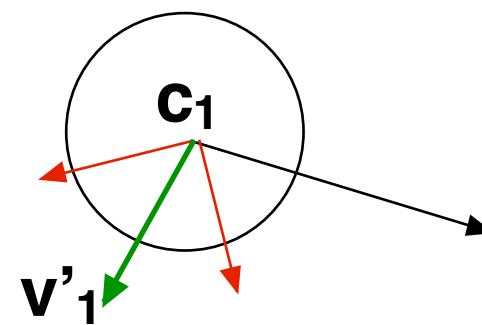
## Collision handling sphere-sphere (simplified, point masses)



Separate - move object away along vector through centers



Split velocities along vector through centers ( $c_2 - c_1$ )



Elastic: Exchange components along  $c_2 - c_1$



# **Beyond point-mass mechanics**

**Rigid body mechanics**

**Better integration**

**Stacking**

**Applying forces and backing time to avoid  
overlap**

**Deformable bodies**

**Breakable bodies**



## **Conclusions, collision detection**

**Must focus on convex shapes**

**Simple collision detection with AABB or  
spheres. Spheres vs polyhedra also easy.  
Polyhedra vs polyhedra hard to do.**

**Global phase also important**

**Narrow phase expensive and complex**