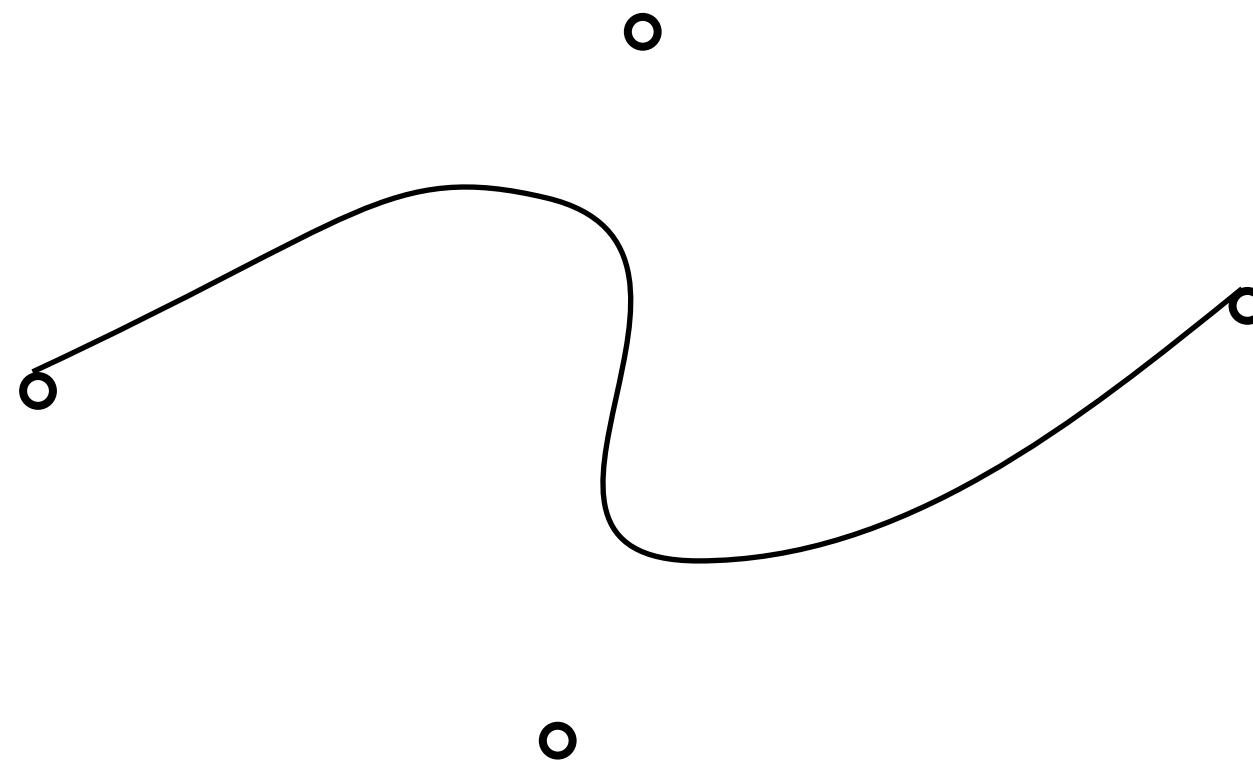




# Bézier curves

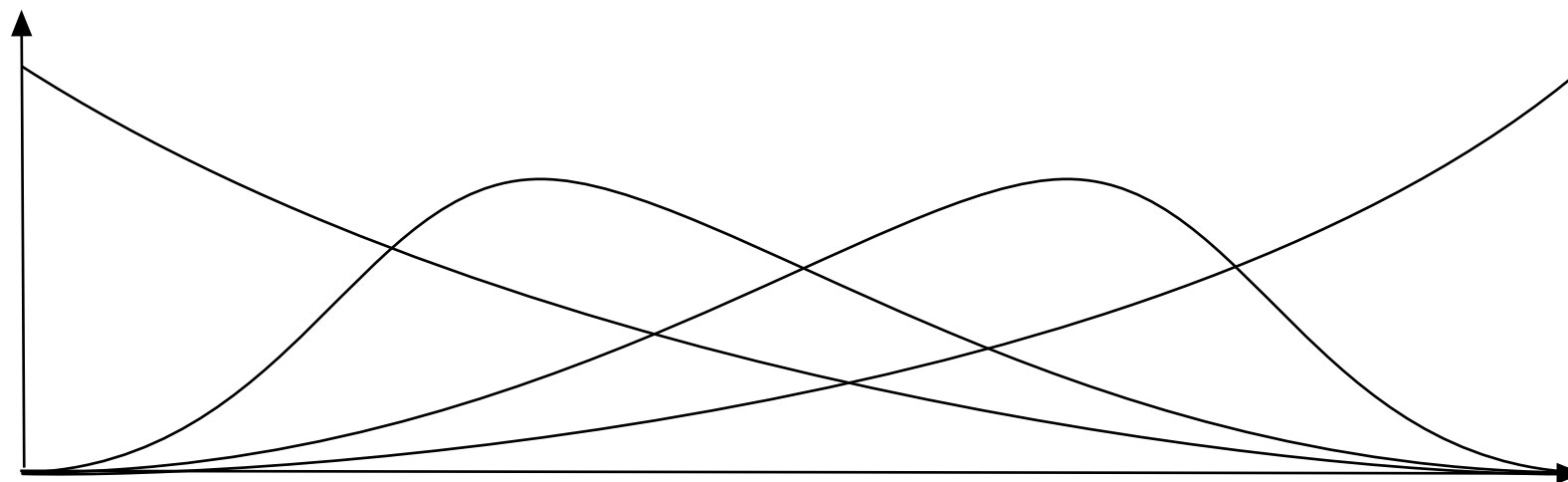
**Typically uses 3 or 4 control points per section**





# Bézier curves

**The 4 points are blended together using 4  
blending functions**





# Bézier curves

**Blending functions:  
Bernstein polynomials**

$$\mathbf{BEZ}_{0,3} = (1-u)^3$$

$$\mathbf{BEZ}_{1,3} = 3u(1-u)^2$$

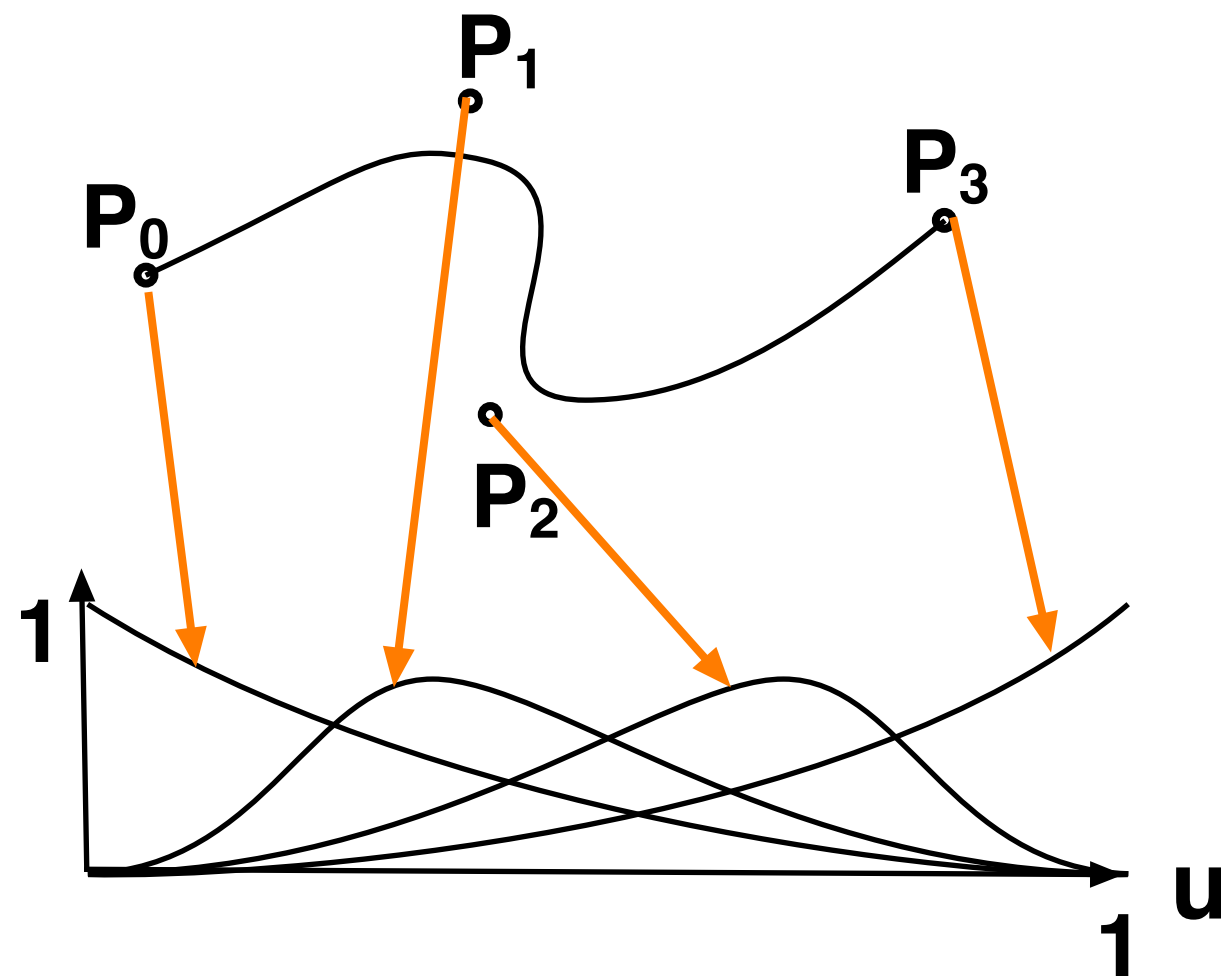
$$\mathbf{BEZ}_{2,3} = 3(1-u)u^2$$

$$\mathbf{BEZ}_{3,3} = u^3$$

**The sum is 1 for any u**



# Information Coding / Computer Graphics, ISY, LiTH



$$\begin{aligned} \text{BEZ}_{0,3} &= (1-u)^3 \\ \text{BEZ}_{1,3} &= 3u(1-u)^2 \\ \text{BEZ}_{2,3} &= 3(1-u)u^2 \\ \text{BEZ}_{3,3} &= u^3 \end{aligned}$$

$$\begin{aligned} P(u) &= P_0 * (1-u)^3 + P_1 * 3u(1-u)^2 + P_2 * 3(1-u)u^2 + P_3 * u^3 \\ &= \sum_{i=0}^3 P_i * \text{BEZ}_{i,3}(u) \end{aligned}$$



## Fitting together sections

**$C_0/G_0$  continuity: just fit the points**

**$C_1$  continuity: Tangents are equal along the edge.**

**$G_1$  continuity: Tangents have same direction along the edge.**

**Simple method: Put 3 points in a line**

