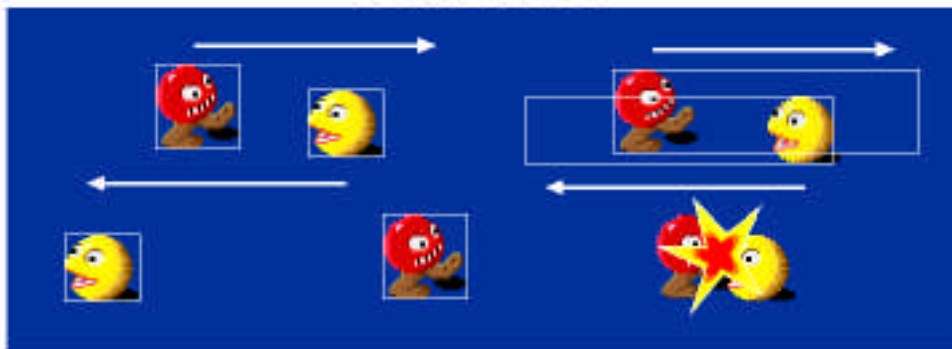




## Moving objects

Fast moving objects may pass right through each other.



Wrong

Right

An example of *temporal aliasing*



## Fast-moving objects

- Test with elongated shapes (sweeping)
- Test several times along the trajectory (multisampling)



## Collision handling

What to do once a collision is found.

- Separate
- Change velocities
- Deform
- Maintain constraints

Full (narrow-phase) tests are hard to resolve.



## Simple particle physics (again)

acceleration = gravity + forces/mass

speed = speed + acceleration

position = position + speed

$$a = g + \sum f/m$$

$$s = s + a$$

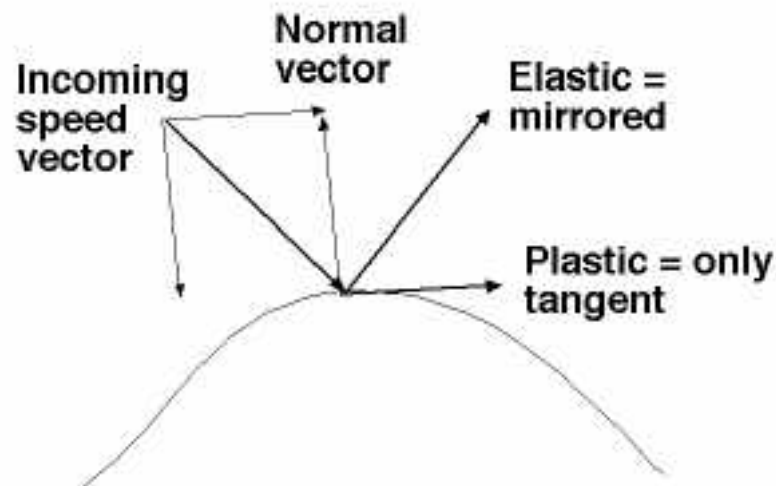
$$p = p + s$$

(“Euler integration”)

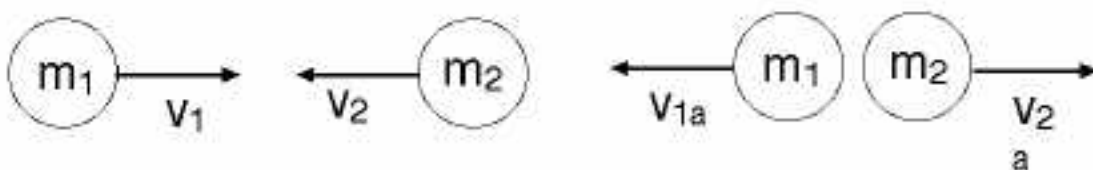
Modify speed and position in collisions



## Simple particle-surface collision



## Plastic and elastic collisions



Preserve momentum

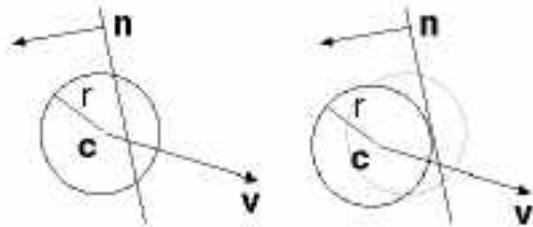
$$m_1 v_1 + m_2 v_2 = m_1 v_{1a} + m_2 v_{2a}$$

Elastic collisions also preserve kinetic energy

$$m_1 v_1^2 + m_2 v_2^2 = m_1 v_{1a}^2 + m_2 v_{2a}^2$$

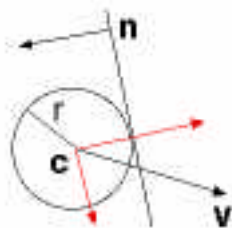


## Collision handling sphere-polyhedra

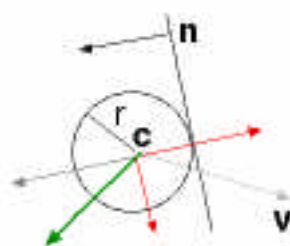


Assuming stationary polyhedra

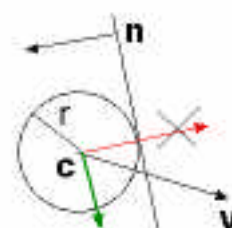
Separate - move object away along normal vector



Split velocity along  $n$



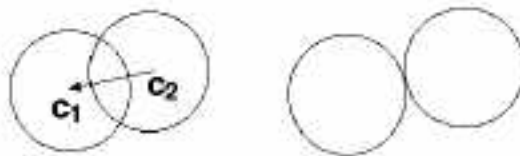
Elastic



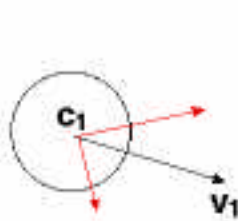
Plastic



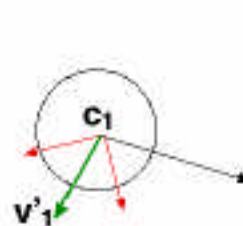
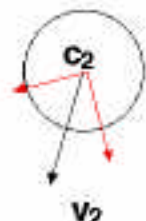
## Collision handling sphere-sphere (simplified, point masses)



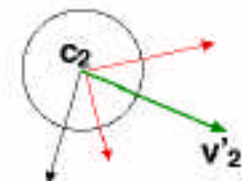
Separate - move object away along vector through centers



Split velocities along vector through centers ( $c_2 - c_1$ )



Elastic: Exchange components along  $c_2 - c_1$





## **Beyond point-mass mechanics**

**Rigid body mechanics**

**Better integration**

**Stacking**

**Applying forces and backing time to avoid  
overlap**

**Deformable bodies**

**Breakable bodies**